Module 6: Process Synchronization

- Background
- The Critical-Section Problem
- Synchronization Hardware
- Semaphores
- Classical Problems of Synchronization
- Critical Regions
- Monitors
- Synchronization in Solaris 2
- Atomic Transactions

Background

- Concurrent access to shared data may result in data inconsistency.
- Maintaining data consistency requires mechanisms to ensure the orderly execution of cooperating processes.
- Shared-memory solution to bounded-buffer problem (Chapter 4) allows at most \( n - 1 \) items in buffer at the same time. A solution, were all \( N \) buffers are used is not simple.
  - Suppose that we modify the producer-consumer code by adding a variable \( counter \), initialized to 0 and incremented each time a new item is added to the buffer.
**Bounded-Buffer**

- **Shared data**
  
  ```
  type item = ... ;
  var buffer: array [0..n-1] of item;
  in, out: 0..n-1;
  counter: 0..n;
  in, out, counter := 0;
  ```

- **Producer process**
  
  ```
  repeat
      ...
      produce an item in nextp
      ...
      while counter = n do no-op;
      buffer[in] := nextp;
      in := in + 1 mod n;
      counter := counter + 1;
  until false;
  ```

**Bounded-Buffer (Cont.)**

- **Consumer process**
  
  ```
  repeat
      while counter = 0 do no-op;
      nextc := buffer[out];
      out := out + 1 mod n;
      counter := counter - 1;
      ...
      consume the item in nextc
      ...
  until false;
  ```

- **The statements:**
  - `counter := counter +1;`
  - `counter := counter - 1;`
  
  must be executed *atomically.*
The Critical-Section Problem

- $n$ processes all competing to use some shared data
- Each process has a code segment, called *critical section*, in which the shared data is accessed.
- Problem – ensure that when one process is executing in its critical section, no other process is allowed to execute in its critical section.
- Structure of process $P_i$

```plaintext
repeat
  entry section
  critical section
  exit section
  remainder section
until false;
```

Solution to Critical-Section Problem

1. **Mutual Exclusion.** If process $P_i$ is executing in its critical section, then no other processes can be executing in their critical sections.

2. **Progress.** If no process is executing in its critical section and there exist some processes that wish to enter their critical section, then the selection of the processes that will enter the critical section next cannot be postponed indefinitely.

3. **Bounded Waiting.** A bound must exist on the number of times that other processes are allowed to enter their critical sections after a process has made a request to enter its critical section and before that request is granted.
   - Assume that each process executes at a nonzero speed.
   - No assumption concerning *relative* speed of the $n$ processes.
Initial Attempts to Solve Problem

- Only 2 processes, \( P_0 \) and \( P_1 \)
- General structure of process \( P_i \) (other process \( P_j \))

\[
\text{repeat} \\
\quad \text{entry section} \\
\quad \text{critical section} \\
\quad \text{exit section} \\
\quad \text{remainder section} \\
\text{until false;}
\]

- Processes may share some common variables to synchronize their actions.

Algorithm 1

- Shared variables:
  - \textbf{var} \( turn : (0..1) \); initially \( turn = 0 \)
  - \( turn = i \Rightarrow P_i \) can enter its critical section
- Process \( P_i \)

\[
\text{repeat} \\
\quad \textbf{while} \, turn \neq i \, \text{do no-op;} \\
\quad \text{critical section} \\
\quad turn := j; \\
\quad \text{remainder section} \\
\text{until false;}
\]

- Satisfies mutual exclusion, but not progress.
Algorithm 2

- Shared variables
  - var flag: array [0..1] of boolean;
    initially flag[0] = flag[1] = false.
  - flag[i] = true ⇒ Pi ready to enter its critical section
- Process Pi
  repeat
    flag[i] := true;
    while flag[j] do no-op;
    critical section
    flag[i] := false;
    remainder section
  until false;

- Satisfies mutual exclusion, but not progress requirement.

Algorithm 3

- Combined shared variables of algorithms 1 and 2.
- Process Pi
  repeat
    flag[i] := true;
    turn := j;
    while (flag[j] and turn=j) do no-op;
    critical section
    flag[i] := false;
    remainder section
  until false;

- Meets all three requirements; solves the critical-section problem for two processes.
Bakery Algorithm

Critical section for $n$ processes

- Before entering its critical section, process receives a number. Holder of the smallest number enters the critical section.
- If processes $P_i$ and $P_j$ receive the same number, if $i < j$, then $P_i$ is served first; else $P_j$ is served first.
- The numbering scheme always generates numbers in increasing order of enumeration; i.e., $1,2,3,3,3,3,4,5...$

Notation

- $<$ ≡ lexicographical order (ticket #, process id #)
  - $(a,b) < (c,d)$ if $a < c$ or if $a = c$ and $b < d$
  - $\max(a_0, \ldots, a_{n-1})$ is a number, $k$, such that $k \geq a_i$ for $i = 0, \ldots, n-1$

- Shared data

  \textbf{var} choosing: array [0..n-1] of boolean;
  number: array [0..n-1] of integer;

  Data structures are initialized to \textit{false} and 0, respectively
Bakery Algorithm (Cont.)

repeat

choosing[i] := true;
number[i] := max(number[0], number[1], ..., number[n - 1])+1;
choosing[i] := false;
for j := 0 to n - 1
do begin
    while choosing[j] do no-op;
    while number[j] ≠ 0
        and (number[j], j) < (number[i], i) do no-op;
end;
critical section
number[i] := 0;
remainder section
until false;

Synchronization Hardware

- Test and modify the content of a word atomically.

function Test-and-Set (var target: boolean): boolean;
begin
    Test-and-Set := target;
    target := true;
end;
Mutual Exclusion with Test-and-Set

- Shared data: var lock: boolean (initially false)
- Process $P_i$

  repeat
  while Test-and-Set(lock) do no-op;
  critical section
  lock := false;
  remainder section
  until false;

Semaphore

- Synchronization tool that does not require busy waiting.
- Semaphore $S$ – integer variable
- can only be accessed via two indivisible (atomic) operations

  $\text{wait}(S)$: while $S \leq 0$ do no-op;
  $S := S - 1$;

  $\text{signal}(S)$: $S := S + 1$;
Example: Critical Section for $n$ Processes

- Shared variables
  - $\text{var} \mutex : \text{semaphore}$
  - initially $\mutex = 1$

- Process $P_i$

  \[
  \text{repeat} \\
  \quad \text{wait}(\mutex); \\
  \quad \text{critical section} \\
  \quad \text{signal}(\mutex); \\
  \quad \text{remainder section} \\
  \text{until false;}
  \]

Semaphore Implementation

- Define a semaphore as a record

  \[
  \text{type} \ semaphore = \text{record} \\
  \quad \text{value: integer;}
  \quad \text{L: list of process;}
  \text{end;}
  \]

- Assume two simple operations:
  - $\text{block}$ suspends the process that invokes it.
  - $\text{wakeup}(P)$ resumes the execution of a blocked process $P$.  

Implementation (Cont.)

- Semaphore operations now defined as

  \[
  \text{wait}(S): \quad S.value := S.value - 1; \\
  \quad \text{if } S.value < 0 \quad \text{then begin} \\
  \quad \quad \text{add this process to } S.L; \\
  \quad \quad \text{block}; \\
  \quad \text{end}; \\
\]

  \[
  \text{signal}(S): \quad S.value := S.value + 1; \\
  \quad \text{if } S.value \leq 0 \quad \text{then begin} \\
  \quad \quad \text{remove a process } P \text{ from } S.L; \\
  \quad \quad \text{wakeup}(P); \\
  \quad \text{end};
\]

Semaphore as General Synchronization Tool

- Execute \( B \) in \( P_j \) only after \( A \) executed in \( P_i \)
- Use semaphore \( flag \) initialized to 0
- Code:

\[
\begin{align*}
  P_i & \quad \quad \quad P_j \\
  \vdots & \quad \quad \quad \vdots \\
  A & \quad \quad \quad \text{wait(flag)} \\
  \text{signal(flag)} & \quad \quad \quad B
\end{align*}
\]
Deadlock and Starvation

- Deadlock – two or more processes are waiting indefinitely for an event that can be caused by only one of the waiting processes.

- Let $S$ and $Q$ be two semaphores initialized to 1

\[
\begin{align*}
P_0 & \quad P_1 \\
wait(S) & \quad wait(Q) \\
wait(Q) & \quad wait(S) \\
\vdots & \quad \vdots \\
signal(S) & \quad signal(Q) \\
signal(Q) & \quad signal(S)
\end{align*}
\]

- Starvation – indefinite blocking. A process may never be removed from the semaphore queue in which it is suspended.

Two Types of Semaphores

- **Counting** semaphore – integer value can range over an unrestricted domain.

- **Binary** semaphore – integer value can range only between 0 and 1; can be simpler to implement.

- Can implement a counting semaphore $S$ as a binary semaphore.
Implementing $S$ as a Binary Semaphore

- Data structures:

  ```
  var
  S1: binary-semaphore;
  S2: binary-semaphore;
  S3: binary-semaphore;
  C: integer;
  ```

- Initialization:

  
  $S1 = S3 = 1$
  $S2 = 0$
  $C = \text{initial value of semaphore } S.$

Implementing $S$ (Cont.)

- `wait` operation

  ```
  wait(S3);
  wait(S1);
  C := C - 1;
  if $C < 0$
  then begin
    signal(S1);
    wait(S2);
  end
  else signal(S1);
  signal(S3);
  ```

- `signal` operation

  ```
  wait(S1);
  C := C + 1;
  if $C \leq 0$ then signal(S2);
  signal(S1);
  ```
Classical Problems of Synchronization

- Bounded-Buffer Problem
- Readers and Writers Problem
- Dining-Philosophers Problem

Bounded-Buffer Problem

- Shared data

```plaintext
type item = ...  
var buffer = ...  
    full, empty, mutex: semaphore;  
    nextp, nextc: item;  
    full := 0; empty := n; mutex := 1;  
```
Bounded-Buffer Problem (Cont.)

- Producer process

```plaintext
repeat
  ...
  produce an item in nextp
  ...
  wait(empty);
  wait(mutex);
  ...
  add nextp to buffer
  ...
  signal(mutex);
  signal(full);
until false;
```

- Consumer process

```plaintext
repeat
  wait(full);
  wait(mutex);
  ...
  remove an item from buffer to nextc
  ...
  signal(mutex);
  signal(empty);
  ...
  consume the item in nextc
  ...
until false;
```
Readers–Writers Problem

- Shared data

\[ \text{var } \text{mutex, wrt: semaphore } (= 1); \]
\[ \text{readcount : integer } (= 0); \]

- Writer process

\[ \text{wait(wrt);} \]
\[ \ldots \]
\[ \text{writing is performed} \]
\[ \ldots \]
\[ \text{signal(wrt);} \]

Readers–Writers Problem (Cont.)

- Reader process

\[ \text{wait(mutex);} \]
\[ \text{readcount := readcount + 1;} \]
\[ \text{if readcount = 1 then wait(wrt);} \]
\[ \text{signal(mutex);} \]
\[ \ldots \]
\[ \text{reading is performed} \]
\[ \ldots \]
\[ \text{wait(mutex);} \]
\[ \text{readcount := readcount - 1;} \]
\[ \text{if readcount = 0 then signal(wrt);} \]
\[ \text{signal(mutex);} \]
Dining-Philosophers Problem

- Shared data

\[
\text{var } \text{chopstick: array [0..4] of semaphore;}
\]
\[
(=1 \text{ initially})
\]

Dining-Philosophers Problem (Cont.)

- Philosopher \( i \):

\[
\text{repeat}
\]
\[
\quad \text{wait(} \text{chopstick}[i] \text{);} \\
\quad \text{wait(} \text{chopstick}[i+1 \mod 5] \text{);} \\
\quad \ldots \\
\quad \text{eat} \\
\quad \ldots \\
\quad \text{signal(} \text{chopstick}[i] \text{);} \\
\quad \text{signal(} \text{chopstick}[i+1 \mod 5] \text{);} \\
\quad \ldots \\
\quad \text{think} \\
\quad \ldots \\
\quad \text{until false;}
\]
Critical Regions

- High-level synchronization construct
- A shared variable $v$ of type $T$, is declared as:

$$\text{var } v: \text{shared } T$$

- Variable $v$ accessed only inside statement:

$$\text{region } v \text{ when } B \text{ do } S$$

where $B$ is a Boolean expression. While statement $S$ is being executed, no other process can access variable $v$.

Critical Regions (Cont.)

- Regions referring to the same shared variable exclude each other in time.
- When a process tries to execute the region statement, the Boolean expression $B$ is evaluated. If $B$ is true, statement $S$ is executed. If it is false, the process is delayed until $B$ becomes true and no other process is in the region associated with $v$. 
Example – Bounded Buffer

- Shared variables:

  ```
  var buffer: shared record
    pool: array [0..n−1] of item;
    count,in,out: integer;
  end;
  ```

- Producer process inserts `nextp` into the shared buffer

  ```
  region buffer when count < n
  do begin
    pool[in] := nextp;
    in := in +1 mod n;
    count := count +1;
  end;
  ```

Bounded Buffer Example (Cont.)

- Consumer process removes an item from the shared buffer and puts it in `nextc`

  ```
  region buffer when count > 0
  do begin
    nextc := pool[out];
    out := out +1 mod n;
    count := count − 1;
  end;
  ```
Implementation: region \( x \text{ when } B \text{ do } S \)

- Associate with the shared variable \( x \), the following variables:

\[
\text{var} \quad \text{mutex, first-delay, second-delay: semaphore;}
\]
\[
\text{first-count, second-count: integer;}
\]

- Mutually exclusive access to the critical section is provided by \( \text{mutex} \).

- If a process cannot enter the critical section because the Boolean expression \( B \) is false, it initially waits on the \( \text{first-delay} \) semaphore; moved to the \( \text{second-delay} \) semaphore before it is allowed to reevaluate \( B \).

Implementation (Cont.)

- Keep track of the number of processes waiting on \( \text{first-delay} \) and \( \text{second-delay} \), with \( \text{first-count} \) and \( \text{second-count} \) respectively.

- The algorithm assumes a FIFO ordering in the queueing of processes for a semaphore.

- For an arbitrary queueing discipline, a more complicated implementation is required.
wait(mutex);
while not B do begin
  first-count := first-count + 1;
  if second-count > 0 then signal(second-delay)
  else signal(mutex);
  wait(first-delay);
  first-count := first-count - 1;
  second-count := second-count + 1;
  if first-count > 0 then signal(first-delay)
  else signal(second-delay);
  wait(second-delay);
  second-count := second-count - 1;
end;

S:
if first-count > 0 then signal(first-delay);
else if second-count > 0 then signal(second-delay);
else signal(mutex);

**Monitors**

- High-level synchronization construct that allows the safe sharing of an abstract data type among concurrent processes.

```
type monitor-name = monitor
variable declarations
procedure entry P1 ( ... );
  begin ... end;
procedure entry P2 ( ... );
  begin ... end;
...
procedure entry Pn ( ... );
  begin ... end;
begin
  initialization code
end.
```
Monitors (Cont.)

- To allow a process to wait within the monitor, a *condition* variable must be declared, as:

  
  ```
  var x,y: condition
  ```

- Condition variable can only be used with the operations *wait* and *signal*.
  - The operation `x.wait;`
    means that the process invoking this operation is suspended until another process invokes `x.signal;`
  - The `x.signal` operation resumes exactly one suspended process. If no process is suspended, then the *signal* operation has no effect.

Dining Philosophers Example

```

type dining-philosophers = monitor

var state : array [0..4] of (thinking, hungry, eating);
var self : array [0..4] of condition;
procedure entry pickup (i: 0..4);
begin
  state[i] := hungry;
  test (i);
  if state[i] ≠ eating then self[i].wait;
end;

procedure entry putdown (i: 0..4);
begin
  state[i] := thinking;
  test (i+4 mod 5);
  test (i+1 mod 5);
end;
```

```
Dining Philosophers (Cont.)

procedure test (k: 0..4);
begin
  if state[k+4 mod 5] ≠ eating
    and state[k] = hungry
    and state[k+1 mod 5] ≠ eating
  then begin
      state[k] := eating;
      self[k].signal;
    end;
end;

begin
  for i := 0 to 4
    do state[i] := thinking;
end.

Monitor Implementation Using Semaphores

- Variables
  var mutex: semaphore (init = 1)
  next: semaphore (init = 0)
  next-count: integer (init = 0)

- Each external procedure F will be replaced by
  
  wait(mutex);
  ...
  body of F;
  ...
  if next-count > 0
    then signal(next)
    else signal(mutex);

- Mutual exclusion within a monitor is ensured.
Monitor Implementation (Cont.)

- For each condition variable $x$, we have:

$$\text{var}\ x\text{-sem: semaphore (init = 0)}$$
$$x\text{-count: integer (init = 0)}$$

- The operation $x$.wait can be implemented as:

$$x\text{-count} := x\text{-count} + 1;$$
$$\text{if}\ \text{next-count} > 0$$
$$\text{then}\ \text{signal(}\text{next}\text{)}$$
$$\text{else}\ \text{signal(}\text{mutex}\text{)};$$
$$\text{wait(}\text{x-sem}\text{);}$$
$$x\text{-count} := x\text{-count} - 1;$$

Monitor Implementation (Cont.)

- The operation $x$.signal can be implemented as:

$$\text{if}\ x\text{-count} > 0$$
$$\text{then begin}$$
$$\text{next-count} := \text{next-count} + 1;$$
$$\text{signal(}\text{x-sem}\text{);}$$
$$\text{wait(}\text{next}\text{);}$$
$$\text{next-count} := \text{next-count} - 1;$$
$$\text{end;}$$
Monitor Implementation (Cont.)

- *Conditional-wait* construct: `x.wait(c);
  - `c` – integer expression evaluated when the wait operation is executed.
  - value of `c` (priority number) stored with the name of the process that is suspended.
  - when `x.signal` is executed, process with smallest associated priority number is resumed next.

- Check two conditions to establish correctness of system:
  - User processes must always make their calls on the monitor in a correct sequence.
  - Must ensure that an uncooperative process does not ignore the mutual-exclusion gateway provided by the monitor, and try to access the shared resource directly, without using the access protocols.

Solaris 2 Operating System

- Implements a variety of locks to support multitasking, multithreading (including real-time threads), and multiprocessing.
- Uses adaptive mutexes for efficiency when protecting data from short code segments.
- Uses condition variables and readers–writers locks when longer sections of code need access to data.
Atomic Transactions

- **Transaction** – program unit that must be executed atomically; that is, either all the operations associated with it are executed to completion, or none are performed.
- Must preserve atomicity despite possibility of failure.
- We are concerned here with ensuring transaction atomicity in an environment where failures result in the loss of information on volatile storage.

Log-Based Recovery

- **Write-ahead log** – all updates are recorded on the log, which is kept in stable storage; log has following fields:
  - transaction name
  - data item name, old value, new value
- The log has a record of `<T_i starts>`, and either
  - `<T_i commits>` if the transactions commits, or
  - `<T_i aborts>` if the transaction aborts.
Log-Based Recovery (Cont.)

- Recovery algorithm uses two procedures:
  - $\text{undo}(T_i)$ – restores value of all data updated by transaction $T_i$ to the old values. It is invoked if the log contains record $<T_i \text{ starts}>$, but not $<T_i \text{ commits}>$.
  - $\text{redo}(T_i)$ – sets value of all data updated by transaction $T_i$ to the new values. It is invoked if the log contains both $<T_i \text{ starts}>$ and $<T_i \text{ commits}>$.

Checkpoints – Reduce Recovery Overhead

1. Output all log records currently residing in volatile storage onto stable storage.
2. Output all modified data residing in volatile storage to stable storage.
3. Output log record $<\text{checkpoint}>$ onto stable storage.

- Recovery routine examines log to determine the most recent transaction $T_i$ that started executing before the most recent checkpoint took place.
  - Search log backward for first $<\text{checkpoint}>$ record.
  - Find subsequent $<T_i \text{ start}>$ record.
- $\text{redo}$ and $\text{undo}$ operations need to be applied to only transaction $T_i$ and all transactions $T_j$ that started executing after transaction $T_i$. 
Concurrent Atomic Transactions

- **Serial schedule** – the transactions are executed sequentially in some order.

- Example of a serial schedule in which $T_0$ is followed by $T_1$:

<table>
<thead>
<tr>
<th></th>
<th>$T_0$</th>
<th>$T_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>read($A$)</td>
<td>read($A$)</td>
</tr>
<tr>
<td></td>
<td>write($A$)</td>
<td>write($A$)</td>
</tr>
<tr>
<td></td>
<td>read($B$)</td>
<td>read($B$)</td>
</tr>
<tr>
<td></td>
<td>write($B$)</td>
<td>write($B$)</td>
</tr>
</tbody>
</table>

Concurrent Atomic Transactions (Cont.)

- **Conflicting operations** – $O_i$ and $O_j$ conflict if they access the same data item, and at least one of these operations is a write operation.

- **Conflict serializable** schedule – schedule that can be transformed into a serial schedule by a series of swaps of nonconflicting operations.
Example of a Concurrent Serializable Schedule

<table>
<thead>
<tr>
<th></th>
<th>$T_0$</th>
<th>$T_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>read</td>
<td>(A)</td>
<td>read(A)</td>
</tr>
<tr>
<td>write</td>
<td>(A)</td>
<td>write(A)</td>
</tr>
<tr>
<td>read</td>
<td>(B)</td>
<td>read(B)</td>
</tr>
<tr>
<td>write</td>
<td>(B)</td>
<td>write(B)</td>
</tr>
</tbody>
</table>

Concurrent Atomic Transactions (Cont.)

- **Locking protocol** governs how locks are acquired and released; data item can be locked in following modes:
  - **Shared**: If $T_i$ has obtained a shared-mode lock on data item $Q$, then $T_i$ can read this item, but it cannot write $Q$.
  - **Exclusive**: If $T_i$ has obtained an exclusive-mode lock on data item $Q$, then $T_i$ can both read and write $Q$.

- **Two-phase locking protocol**
  - **Growing phase**: A transaction may obtain locks, but may not release any lock.
  - **Shrinking phase**: A transaction may release locks, but may not obtain any new locks.

- The two-phase locking protocol ensures conflict serializability, but does not ensure freedom from deadlock.
Concurrent Atomic Transactions (Cont.)

- *Timestamp-ordering* scheme – transaction ordering protocol for determining serializability order.
  - With each transaction $T_i$ in the system, associate a unique fixed timestamp, denoted by $TS(T_i)$.
  - If $T_i$ has been assigned timestamp $TS(T_i)$, and a new transaction $T_j$ enters the system, then $TS(T_i) < TS(T_j)$.

- Implement by assigning two timestamp values to each data item $Q$.
  - **W-timestamp**($Q$) – denotes largest timestamp of any transaction that executed write($Q$) successfully.
  - **R-timestamp**($Q$) – denotes largest timestamp of any transaction that executed read($Q$) successfully.

Schedule Possible under Timestamp Protocol

<table>
<thead>
<tr>
<th>$T_2$</th>
<th>$T_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>read($B$)</td>
<td>read($B$)</td>
</tr>
<tr>
<td></td>
<td>write($B$)</td>
</tr>
<tr>
<td>read($A$)</td>
<td>read($A$)</td>
</tr>
<tr>
<td></td>
<td>write($A$)</td>
</tr>
</tbody>
</table>

- There are schedules that are possible under the two-phase locking protocol but are not possible under the timestamp protocol, and vice versa.
- The timestamp-ordering protocol ensures conflict serializability; conflicting operations are processed in timestamp order.